

# Climate risk and financial stability in the network of banks and investment funds\*

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## Abstract

We develop a method to analyze the effects on financial stability of the interplay between climate policy shocks and market conditions. We combine the frameworks of the Climate Stress-test with the framework of the network valuation of financial assets, in which the valuation of interbank claims accounts for market volatility as well as for endogenous recovery rates consistent with the network of obligations. We also include the dynamics of common asset contagion involving not only banks but also investment funds, which are key players in the low carbon transition. We then apply the model to a unique supervisory data-set of banks and investment funds at the firm level in order to assess the impact for financial stability of shocks deriving from the disorderly alignment of energy and utility sectors in a range of climate policy scenarios. While under mild shock scenarios systemic losses are contained, we identify the climate policy scenarios and market conditions under which systemic losses can pose a threat to financial stability.

Keywords: financial stability, climate risk, sustainable finance, climate stress-test, low-carbon transition risk, 2°C opportunities, JEL Codes: D85, D86, E58, G01, Q54

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## 1 Introduction

In the view of many academic scholars and experts from the private sector, there is a growing gap between climate objectives and the allocation of financial capital. Narrowing this gap requires to enhance the standard financial metrics to encompass climate risk. Moreover, given the interconnect-edness of today's business, these enhanced metrics of risk and impact need to be based on network models of both investment chains and supply chains.

In the last months, the relationship between climate risk and financial stability has taken center stage in the policy debate. On the one hand, there is evidence from several countries of the growing opportunities for green sectors along 2-degree compatible trajectories. On the other hand, in other countries, risk can build up from the increasing misalignment between the current trajectories of some sectors of the economy and the trajectories required by the 2°C targets, as set out in the context of the 2015 Paris Agreement. While the importance of the topic is now widely recognised and a stream of work on financial stability builds on the recent concept of climate stress-test of the financial system, several crucial issues remain unaddressed.

The impact on financial stability of the interplay between climate policy shocks and market conditions has not been analysed so far. In this paper, we develop a method to analyze these effects in a systematic way. We also provide a graphic method, the *climate envelope scenario analysis*, to compare bundles of trajectories related to different climate policy shock scenarios and market conditions scenarios. To this end, we combine the frameworks of the Climate Stress-test with the framework of the network valuation of financial assets, in which the valuation of interbank claims accounts for market volatility as well as for endogenous recovery rates consistent with the network of obligations.

Existing stress-testing frameworks have focused so far on the banking system. However, the banking sector is little exposed, in a direct way, to the economic sectors that are most relevant for the low-carbon transition. In contrast, investment funds have been found by previous empirical analyses, to be at the same time much more exposed to climate relevant sector as well as to be a crucial sector for scaling up the investments needed to finance the low-carbon transition. To the best of our knowledge, the combined effect of banks and investment funds has not been studied so far. Additionally,

in some countries like Mexico, development banks could also play a relevant role in the low carbon transition and their impact on financial stability has only been seldom analyzed so far (Monasterolo et al., 2018). In this paper, we address this issue by developing a stress-test model that encompasses at the same time banks and investment funds.

So far, most of the models to estimate losses arising from financial contagion have focused on distress contagion and common exposures contagion separately. In this paper we show that the combination of the two effects gives rise to losses that are larger than the sum of the individual contributions. This result implies that not considering the interplay between the two channels of financial contagion underestimates systemic risk. We address this issue by extending the NEVA framework by (Barucca et al., 2016) including the liquidation of common assets mechanism.

The climate stress test methodology has been only based on the DebtRank model so far (Battiston et al., 2012b; Bardoscia et al., 2015), without including more recent extensions of financial contagion models. In this paper, we address this issue by extending the concept of climate stress test to the NEVA framework in order to account for the ex-ante valuation of financial assets and market volatility in a set of climate policy scenarios.

This work is related to several streams of literature which are mentioned and discussed in the relevant subsections of the Section 2 and deal respectively with climate risk and financial stability, stress-frameworks and models of financial contagion in the banking system, both via direct contagion and via common asset exposures.

In this work, we leverage on a unique supervisory dataset from Banco de Mexico detailing for the first time the interconnections among investment funds and the banking sector (including brokerage houses and development banks) at the level of individual institutions, as well as their exposures to non-financial firms at the level of individual securities.

We first develop an extended stress-test framework that encompasses banks, brokerage houses, development banks and investment funds, by building on previous work of the authors on stress-test frameworks in bank networks (i.e. DebtRank Battiston et al. (2012a), and NEVA Barucca et al. (2016)). In the model, we study the effect of the contagion channel between investment funds and banks. Additionally, investment funds are subject to a balance-sheet contagion mechanism (i.e. building on the insights of Kiyotaki and Moore (2002); Greenwood et al. (2015)) leading to a spiral of deleveraging and fire sales.

Crucially, and differently from traditional stress-test frameworks, we cover the case in which the valuation of financial actors obligations is carried before the maturity of the contracts (NEVA). Our analysis covers extensively the effect of crucial parameters such as the recovery rate coefficient, the volatility of securities and the elasticity of securities prices with respect to the fire sales volume.

We apply this stress-test framework on the dataset of Banco de Mexico to investigate the impact

for financial stability of shocks deriving from the misalignment of energy and utility sectors in a wide range of climate policy scenarios, building on the notion of climate stress-test developed in Battiston et al. (2017).

Our results show that, based on empirical results of a fairly complex and extremely well-documented financial system such as the Mexican one, the exposures (direct and indirect) between banks, brokerage houses and investment funds can in principle be a significant shock transmission channel. This channel has been previously neglected, especially in the context of the low carbon transition of emerging and advanced economies.

The insights from this exercise are relevant to a good extent to EU countries, where such an exercise has not yet been carried out at this level of detail and depth. We discuss the policy implications of our finding and the avenues for future research.

The rest of the paper is structured as follows. In Section 2 we describe the methodology we have developed to carry out the extended climate stress-test analysis. In Section 3 we discuss our data set. In Section 4 we analyze our empirical results, and Section 5 concludes.

## 2 Methods

In this section we provide a short description of the methods we build on and the necessary extensions that were used in this work. Then, we describe the set of operative steps used to carry out the computation.

### 2.1 Climate Stress-test

There are two channels through which climate change can result in risks for public and private financial institutions. On the one hand, physical risk (e.g. damages to physical assets, natural capital, and/or human lives) can result from climate-induced extreme weather events (ICCP, 2014). On the other hand, climate risks could also result from the transition to a low-carbon economy, referred to as transition risk (ESRB, 2016; Batten et al., 2016). In this paper we focus on the impact on financial stability of the latter.

As described in (Monasterolo et al., 2017) there are three important sources of shocks that could limit the ability of market participants to fully anticipate price adjustments of carbon-intense assets. These sources include: i) technological shocks (e.g. renewable energy production costs); ii) scientific discovery shocks (e.g. new evidence on likelihood to miss the 2°C target Rogelj et al. (2016)); iii) climate-relevant policy shocks (e.g., the achievement of COP21 agreement in 2015, or the US withdrawal from the Paris Agreement in 2016).

The first methodology to account for climate-related transition risk in the computation of financial risk metrics for individual financial institutions has been introduced in (Battiston et al., 2017). In particular, the method allows to compute a Climate Value at Risk and to conduct a Climate Stress-Test of both individual institutions and of the whole banking system in a given region. The methodology aims to quantify risk of a disorderly price adjustment in the economic sectors related to energy. It estimates distributions of shocks on a portfolio of investments in non-financial firms in economic sectors that can be affected positively or negatively by late and sudden alignments to climate policies. For instance, within a country that delays its alignment to 2°C targets in terms of composition of its energy production sources (energy mix), the firms in the energy sector that have not adapted to the targets face unanticipated costs associated with the transition. In contrast, firms that have invested in green technologies would profit. Accordingly, financial investments in energy firms reflect positive and negative shocks. Under a set of mild assumptions, the magnitude of these shocks can be related to the characteristics of forward-looking trajectories of output of the various economic sectors. These trajectories are taken from the LIMITS database<sup>1</sup>, which includes all the major scenarios of the economic impact of climate change and climate policies on the energy sectors according to a set of well-established Integrated Assessment Models (Kriegler et al., 2013).

There are two ways to estimate distributions of shocks in sectors' market share from the LIMITS trajectories. The first way uses the longitudinal variation along each trajectory Battiston et al. (2017). The second way uses the variation in market share across trajectories. In this paper, we follow the latter approach, in which each shock is interpreted as the variation in market share of a sector resulting from the country moving from a business-as-usual scenario into one of the possible standard climate policy scenarios (according to IPCC and IEA) in a disorderly way.

### 2.1.1 Policy Scenarios Analysis

In the face of climate risk, there there are two main policy scenarios. Either the transition to a low carbon economy occurs or it does not. We refer as  $P_T$  the probability of the transition to happen. It follows that  $(1 - P_T)$  is the probability of no transition. In case of no transition, the cost of extreme climate events is large and we define it as  $C_{CDH}$ . The goal of the transition is to mitigate climate risk and reduce the cost of extreme climate events to a lower value  $C_{CDL}$ , where  $C_{CDL} < C_{CDH}$  (Carney, 2015). The transition to a low carbon economy can either occur orderly, with probability  $(1 - P_F)$ , or disorderly with probability  $P_F$ . In the first case the cost would be low  $C_{FCL}$ , in the second case it would be high  $C_{FCH}$ . The expected cost of climate risk is

$$\mathbb{E}(\text{Cost of Climate Risk}) = P_T P_F (C_{FCH} + C_{CDL}) + P_T (1 - P_F) (C_{FCL} + C_{CDL}) + (1 - P_T) C_{CDH}. \quad (1)$$

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<sup>1</sup><https://tntcat.iiasa.ac.at/LIMITSDB/dsd?Action=htmlpage&page=about>

However, the probability for the transition to occur is endogenous, as it depends on how the various actors involved (e.g., policy makers, non-financial corporations, financial institutions, and society) perceive the costs in equation 1 (Bretschger and Pattakou, 2018). Since  $P_T < 1$ , it follows that risk neutral agents have an incentive to support the transition if the cost of climate change  $C_{CDH}$  is large enough, i.e.

$$C_{CDH} > P_F(C_{FCH} + C_{CDL}) + (1 - P_F)(C_{FCL} + C_{CDL}). \quad (2)$$

As shown in equation 2, the probability of the transition to happen depends on climate damage cost and the expected cost of the transition. Notice that Equation 2 also depends on the probability of whether the transition happens in an orderly or disorderly way. One could also derive a more general upper bound for transition losses below which it is always better to shift to a low carbon economy. In fact, if the sum of the cost of the transition and the low climate cost in case of mitigation is lower than the large cost of climate in case of no transition, i.e.,

$$C_{CDH} > C_{FCH} + C_{CDL}, \quad (3)$$

market players always have an incentive to support the shift.

In this paper we do not aim to estimate the probabilities  $P_F$  or  $P_T$ , in contrast we focus on estimating the cost for the financial system of a disorderly transition. In particular, we contribute to the policy discussion on climate risk by showing that this cost depends on the interplay between climate policy shocks and market conditions.

## 2.2 Extended Bank-fund climate stress-test

In this paper we extend the models of financial contagion to derive the first climate stress-test methodology that combines an ex-ante valuation of financial assets, an endogenous recovery rate and a fire-sales reaction that consider several types of financial institutions at the same time. The dynamics of contagion can be summarized as follows:

1. **Climate policy shocks:** we estimate the impact of the late and disorderly alignment to a climate policy building on the economic trajectories provided in the LIMITS database. The database provides an estimation of the evolution of the output of different sectors of the real economy in different policy scenarios. We define the climate shock as the difference between the Business as Usual scenario and each climate policy scenarios and we translate it into a shock on the value of bonds and loans.
2. **First round:** we compute the losses suffered by banks and funds due to direct exposures multiplying their exposures towards Climate Policy Relevant Sectors (CPRS) with the LIMITS

shocks Battiston et al. (2016). Financial institutions suffer a set of correlated shocks from multiple asset classes.

3. **Second round:** first we carry out an ex-ante valuation of intra-financial banks' assets due to the first round shock using a generalized model of financial contagion Barucca et al. (2016) which includes an endogenous recovery rate. Second we estimate the devaluation of funds assets due to banks' increased probability of default.
4. **Third round:** we estimate banks' and funds' reaction to the shock in order to get to their initial risk management constraints. In line with Kiyotaki and Moore (2002); Greenwood et al. (2015); Cifuentes et al. (2005), the liquidation suddenly increases the supply on the market further causing losses on banks and funds balance sheets.
5. **Fourth round:** finally we estimate losses that are too large to be absorbed by banks' capital and are transmitted to external creditors Roncoroni et al. (2018).

In this paper we refer to a *shock scenario* as the combination of: i) a *market conditions scenario* i.e., a range of values for the parameters recovery rate  $R$ , market volatility  $\sigma$ , market elasticity  $\alpha$ , and the funds' VaR; and ii) a *climate policy shock scenario*, i.e., a set of shock arising from the late and disorderly alignment from BAU trajectory to a set of climate target trajectories. Therefore the output of the extended climate stress test framework, is a database of trajectories for the systemic losses (see Table 2) in each stage of the contagion process. The novelties of our model with respect to prior models to study financial contagion are illustrated in Table 1 along the following dimensions.

- **Endogenous Recovery Rate.** The term refers to the fact that the recovery rate is computed as the ratio between the face value of an interbank obligation and its value at the equilibrium of the clearing process. (Eisenberg and Noe, 2001) were the first to prove the existence and to determine the conditions for uniqueness of the endogenous recovery rate in a financial network. In the model based on DebtRank the recovery rate is exogenous. Barucca et al. (2016) have shown how to endogenize the recovery rate in the DebtRank framework. This approach has been applied to supervisory data in Roncoroni et al. (2018).
- **Ex-Ante Valuation.** The term refers to a network coherent valuation of financial assets which is carried out before the maturity of contracts. The concept has been introduced by Battiston et al. (2012b) and extended in Barucca et al. (2016) to encompass the case of à la Merton valuation of external assets.
- **Firesales Contagion.** The term refers to losses arising from the sudden liquidation of the exposures to common assets. To encompass firesales contagion in our contagion framework, we

build on the models discussed in Kiyotaki and Moore (2002); Greenwood et al. (2015); Caccioli et al. (2014); Cifuentes et al. (2005); Caballero and Simsek (2013).

- **Investment Funds.** The term refers to the fact that our model also considers investment funds when computing the exposure of the financial system towards climate relevant scenarios and when computing losses arising from financial contagion.
- **Climate Module.** The terms refers to the fact that the initial shocks are triggered by a late and disorderly alignment to climate targets. To estimate the climate policy shocks we build on a long stream of literature that includes Battiston et al. (2017); Monasterolo et al. (2017, 2018); Dietz et al. (2016).

Notice that combining banks and investment funds in the same dynamics of contagion poses some challenges. First, ignoring the exposures of funds towards banks would underestimate the losses that trigger liquidation. Second, by the nature of the asset fire-sales dynamics when including the sudden reaction of a larger set of financial institutions the losses due to price drop spirals are larger.

Literature reference	Model features				
	Endogenous Recovery Rate	Ex-Ante Valuation	Firesales Contagion	Investment Funds	Climate Module
Systemic Risk Eisenberg and Noe, 2001					
DebtRank Battiston ea., 2012					
Leveraging the Network Battiston ea., 2016					
Pathways Bardoscia ea., 2017					
NEtwork VALuation Barucca ea., 2016					
Interconnected Banks Roncoroni ea., 2018					
Climate Stress Test Battiston ea., 2017					
<b>Our work</b> <b>Roncoroni ea., 2019</b>					

Table 1: Overview of literature on financial contagion summarizing the novelty of the methodology introduced in this paper. The color of cells show whether each of the cited papers includes or not each model feature: green means that it includes the feature, white means that it does not include the feature.



### 2.3 Losses due to direct exposure

While Battiston et al. (2017) focuses on the valuation, under climate policy shocks, of equity holdings of banks in firms in the energy and utility sectors, (Monasterolo et al., 2018) focuses on the valuation, under climate policy shocks, of loans to firms in the energy and utility sectors. In our dataset, the majority of exposures of banks in climate relevant sectors are in the forms of loans and corporate bonds. For the investment funds, they are corporate bonds. Therefore, we follow the valuation formula in (Monasterolo et al., 2018).

The valuation works under the following set of assumptions. There are two type of shocks affecting the value of the firms. The first is the policy shock which is deterministic and correlated across firms in a given sector, as it affects the whole sector. The second is an idiosyncratic shock that affects each firm independently (due to management capabilities and productivity shocks specific to the firms). At this stage of the model, we assume that the idiosyncratic shocks on the borrower asset side are drawn from the same distribution, which is assumed to be a non-negative random variable with a continuous, differentiable distribution function. While it is possible to handle computationally any empirical distribution of shocks, we do not have the data at a firm level to do so. For the sake of simplicity, at the current stage of the model, we approximate the distribution of idiosyncratic shocks with a uniform distribution, for a justification of this assumption see also Section 2.4.

We treat loans and bonds in the same way, based on the valuation approach of expected value. Under our mild assumptions, it is shown in Monasterolo et al. (2018) that, conditional to the policy shock, the change in the expected value of a loan reads:

$$\Delta A_{ij} = F_{ij}(1 - r_j) \frac{E_j}{\delta} \chi u_{mpcst} \quad (4)$$

where  $A$  is the expected value of the bond,  $F$  is the face value of the bond,  $r$  is the recovery rate,  $E$  is the equity of the firm,  $\delta$  is the support of the distribution of idiosyncratic shocks,  $\chi$  is the elasticity of profitability in respect to the market share of the sector, and  $u$  is the market share shock,  $m$  labels the model chosen to estimate the trajectory in the climate policy scenario  $p$  at time  $t$  on sector  $s$  of country  $c$ . We thus define the tensor of LIMITS shocks  $L$  as

$$L_{mpcst} = \frac{\Delta A_{ij}}{F_{ij}}, \quad (5)$$

and, as in Monasterolo et al. (2018), setting  $r_j = 0 \forall j$ ,  $\frac{E_j}{\delta} = 1$ , and  $\chi = 1$ .

To direct estimate the impact of the shocks on the value of firms in each sector on banks' and investment funds' exposures we build on (Battiston et al., 2016) and on the tensorial notation from (Roncoroni et al., 2018). The shock absorbed via direct exposure is called first round shock and is

expressed as

$$\Xi_{it}^{1st} = \min \left\{ 0, \sum_c \sum_s \min \{0, L_{mpcst}\} \cdot A_{icst}^{\text{loans, bonds}} + \sum_c \sum_s L_{mpcst} \cdot A_{icst}^{\text{equity}} \right\}, \quad (6)$$

where the index  $i$  labels the financial institution,  $c$  labels the country of the exposure,  $s$  labels the sector of the exposure,  $t$  labels the year of introduction of the policy aimed at mitigating climate change, and  $A$  is the tensor of exposures of financial institutions. While the methodology is able to capture the impact of positive shocks on equity holdings as well, we empirically observe that the majority of banks’ and investment funds’ exposures towards energy sectors are on the form of loans and corporate bonds. Further, since only banks are subject to limited liabilities, the shock suffered by banks is bounded by their initial equity. Notice that, to solve the taxonomy issue, we applied the trajectory of the LIMITS sector “Primary Energy|Fossil” to the CPRS sector “Fossil-Fuel” and the trajectory of the LIMITS sector “Secondary Energy|Electricity|Gas” to the CPRS sector “Utilities”. Additionally, since electricity in Mexico is only partially produced by Gas, we apply a factor 83.16% to the negative shocks.<sup>2</sup>

## 2.4 Network Valuation of Financial Assets

To compute the network coherent devaluation of banks’ bilateral claims we build on (Barucca et al., 2016; Allen and Gale, 2001; Gai and Kapadia, 2010; Roukny et al., 2013; Di Iasio et al., 2013; Tabak et al., 2013; Thurner and Poledna, 2013; Poledna and Thurner, 2016; Fink et al., 2016; Puliga et al., 2014; Bardoscia et al., 2015, 2017; Roncoroni et al., 2018). In particular, we assume that a portion of the non-shocked external assets is subject to market volatility which generates stochastic shocks that follow a uniform distribution, as shown in Roncoroni et al. (2018). In order to account for financial friction, an exogenous recovery rate  $R$  is applied to banks’ payments in order to simulate market imperfections such as legal costs. Figure 1 illustrates with more detail the time dimension of the contagion dynamics. We assume that banks allocate their exposures towards other banks at time  $t_0$ . At time  $t_1$  a known shock, in this case the shock computed using the LIMITS trajectories, modifies the value of the external asset classes reducing the capital of banks. At time  $t$  banks carry out a coherent network valuation of interbank claims that mature at time  $T$ . Between  $t$  and  $T$  a stochastic shock induced by market volatility modifies the value of banks’ external assets further reducing the mark-to-market value of banks’ capital. The probability of banks’ default thus depends on the initial network structure, the deterministic shock as well as on the distribution of the future stochastic shock.

Since the stochastic shock on bonds held by banks is by definition bounded from below at zero

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<sup>2</sup><https://www.iea.org/statistics/monthly/#electricity>

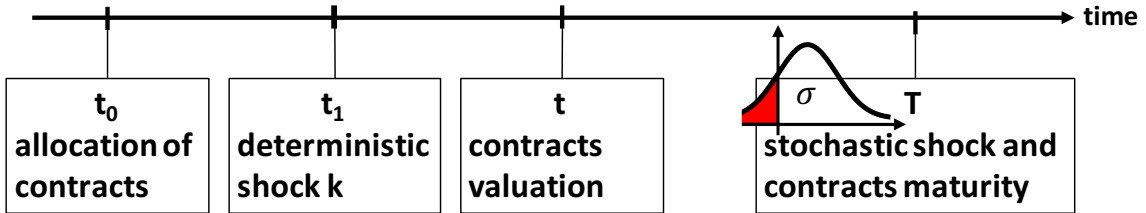


Figure 1: Illustration of the time dimension of the contagion model. At  $t_0$  contracts are written, at time  $t_1$  a known shock reduces the value of banks' external assets, at time  $t$  the valuation is carried out, at time  $T$  the value of banks' external assets is further reduced due to market volatility thus reducing mark-to-market banks' capital.

and from above by the face value, one can not model it using a Gaussian distribution. In order to satisfy those two constraints, we decided to model the stochastic shocks using a beta distribution. Additionally, we assume that banks' have a risk management strategy such that the shocks on their total asset follow a non-convex distribution. This means that they aim to contain the left hand side tail of the distribution. However, since we still want to model extreme events, among all the non-convex beta distribution functions we chose the one that has the heaviest tail (which in the limit of  $\beta(1, 1)$  coincides with the uniform distribution). For all those reasons together, we decided to model the stochastic shocks using a uniform distribution, as for the bonds valuation. A uniform distribution can be uniquely defined by the size of its support. Notice that this is not what it is usually done in the classical (Merton, 1974). However, since the probability of extreme events is by construction higher when modeled with a uniform distribution instead of a log-normal one, the results we obtain from direct contagion when market volatility is large can be considered as an upper bound of losses. In this project we assume that banks are exposed to risk proportionally to their initial capital. We call the proportionality factor "market volatility" and we label it by  $\sigma$ . The stochastic shock is thus uniformly distributed between 0 and  $M_i$ , where

$$M_i = \max\{0, \min\{A_i^e, \sigma E_{0i}\}\}. \quad (7)$$

It is important to notice that the model could still be solved numerically under any empirical distribution. However, for the sake of simplicity and also because of the lack of data, we made the choice that allowed us to solve the problem analytically. While this is a limitation of the current stage of the model, this choice is particularly useful because it allows us to identically recover the (Eisenberg and Noe, 2001) model (setting  $\sigma = 0$  and  $R = 1$ ) and the (Battiston et al., 2012b) model (setting  $\sigma = 1$ ).

Building on (Barucca et al., 2016) we assume that banks' equity is a function of the probability of

default of their counterparties

$$E_i(t) = A_i^e - L_i^e + \sum_{j=1}^N A_{i,j}^b \mathbb{V}_{ij}(\mathbf{E}(t)) - \sum_{j=1}^N L_{i,j} \quad \forall i, \quad (8)$$

where the valuation of interbank claims  $\mathbb{V}$  corresponds to the mark-to-market valuation of financial assets. More precisely

$$\mathbb{V}_{ij}(\mathbf{E}(t)) = 1 - p_j^D(E_j) + R\rho_j(E_j), \quad (9)$$

where  $p_j^D$  is the probability of default of bank  $j$ ,  $R$  is the exogenous recovery rate, and  $\rho_j$  is bank's  $j$  endogenous recovery rate. Banks'  $j$  probability of default is computed as

$$\begin{aligned} p_j^D(E_j) &= \mathbb{E} \left[ \mathbb{1}_{E_j(T) < 0} \right] = \int_0^{M_j} dx \frac{1}{M_j} \mathbb{1}_{x > E_j} = \\ &= \left( 1 - \frac{\max\{0, E_j\}}{M_j} \right) \mathbb{1}_{M_j > E_j}, \end{aligned} \quad (10)$$

where  $x$  is the value of the future stochastic shock induced by market volatility. Similarly, banks endogenous recovery rate is expressed as

$$\begin{aligned} \rho_j(E_j) &= \mathbb{E} \left[ \left( \frac{E_j(T) + \bar{p}_j}{\bar{p}_j} \right)^+ \mathbb{1}_{E_j(T) < 0} \right] = \\ &= \int_0^{M_j} dx \frac{1}{M_j} \left( \frac{E_j - x + \bar{p}_j}{\bar{p}_j} \right) \mathbb{1}_{x > E_j} \mathbb{1}_{E_j - x + \bar{p}_j > 0}, \end{aligned} \quad (11)$$

where  $\bar{p}$  is the vector of total interbank liabilities and the “+” symbol indicates that only the positive part is considered in order to avoid negative payments. For a more exhaustive derivation of the valuation function, including the case when  $\sigma = 0$ , refer to (Roncoroni et al., 2018).

Inserting the valuation vector inside equation (8) one obtains the dynamics to compute the fixed point of the algorithm that identifies the ex-ante valuation of interbank claims which is network coherent and considers future stochastic shocks. Each element of the vector of valuation  $\mathbb{V}$  is bounded between 0 and 1, where 1 means that the loan is paid with probability 100% and 0 means that the counterparty  $j$  will not honor its obligation towards bank  $i$ .

To include other financial institutions, such as investment funds, into the stress test dynamics we assume that their exposure towards banks is mark-to-market. Since we observe empirically funds' exposures towards banks via securities but not the opposite side exposures; and the default of funds is more difficult to model, we compute the losses induced by the increased probability of banks after

interbank contagion. Losses due to indirect exposures are thus written as

$$\Xi_{it}^{2nd} = \sum_j A_{ij}^b \cdot (1 - \mathbb{V}_{ij}(T)), \quad (12)$$

where losses that exceeds banks equity are capped for the same reason as before.

## 2.5 Fire-sales contagion among financial institutions

After absorbing losses due to direct and indirect exposures, the balance sheet of financial institutions is substantially modified. On the one hand banks used their capital to absorb the shock, on the other hand funds are exposed to a new profile of risk. In the spirit of Kiyotaki and Moore (2002); Caballero and Simsek (2013); Diamond and Rajan (2011); Adrian and Shin (2008); Allen et al. (2012); Caccioli et al. (2014); Georg (2013); Tasca and Battiston (2016), we assume that banks react by liquidating part of their portfolio to quickly restore their initial level of leverage.

There is growing interest in the policy community in understanding the role of investment funds in financial stability and in works that model investment banks funds' behaviour in the context of fire sales. To our knowledge, there is very little academic work on this question so far.

There is however, anecdotal evidence that motivates us to model funds decision making based on Value at Risk. Indeed, in Mexico, investment funds are required to disclosure their Value at Risk<sup>3</sup>. Moreover, using Value at Risk for risk management purposes is a common practice also among funds operating in international financial markets.<sup>4</sup>

Therefore, we model funds' decision making by assuming that, conditional upon the shock, they aim to restore their initial level of Value at Risk (VaR). When determining the amount that has to be liquidated in order to restore the initial balance sheet constraints, we assume that each asset class is sold proportionally. Notice that as in Greenwood et al. (2015), we do not allow for a coordinated liquidation among financial institutions.

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<sup>3</sup>See for instance <https://www.cnbv.gob.mx/SECTORES-SUPERVISADOS/SOCIEDADES-DE-INVERSION/Buscador-de-Sociedades-de-Inversi3n/Paginas/Comparador.aspx>

<sup>4</sup>For example, a prospectus from one of Blackrock funds states: "Accordingly the Manager will employ a risk-management process which enables the Manager to monitor and measure at any time the risk of the derivative positions and their contribution to the overall risk profile of a Fund. In these circumstances, the Manager applies a "Value at Risk" approach to calculate a Fund's global exposure and to ensure it complies with the investment restrictions set out in Appendix 3". (from [https://www.blackrock.com/uk/individual/literature/prospectus/blackrock-investment-funds-prospectus.pdf?locale=en\\_GB&switchLocale=y&siteEntryPassthrough=true](https://www.blackrock.com/uk/individual/literature/prospectus/blackrock-investment-funds-prospectus.pdf?locale=en_GB&switchLocale=y&siteEntryPassthrough=true))

### 2.5.1 Fire-sales contagion among banks

After second round shocks, we assume that banks liquidate a portion of their assets in order to recover their initial leverage value. The new value of banks' leverage is

$$\Lambda_{it}^{2nd} = \frac{A_{it}^{2nd}}{E_{it}^{2nd}} = \frac{A_{it} + \Xi_{it}^{1st} + \Xi_{it}^{2nd}}{E_i(0) + \Xi_{it}^{1st} + \Xi_{it}^{2nd}}. \quad (13)$$

When banks liquidate part of their assets, they decrease their leverage for two reasons: (1) they have less exposure, and (2) they increase their capital. By defining  $k$  the portion of total assets that is liquidated, the new level of leverage can be rewritten as

$$\Lambda_{it} = \frac{(1 - k_i) (A_{it} + \Xi_{it}^{1st} + \Xi_{it}^{2nd})}{E_i(0) + \Xi_{it}^{1st} + \Xi_{it}^{2nd} + k_i (A_{it} + \Xi_{it}^{1st} + \Xi_{it}^{2nd})}. \quad (14)$$

Solving equation (14) by  $k_i$  provides the portion of total assets that each bank has to liquidate. Further, we assume that a bank in default is totally liquidated, i.e.,

$$k_i = 1, \quad i \text{ is in default}. \quad (15)$$

### 2.5.2 Fire-sales contagion among funds

Building on (Luu et al., 2018), we assume that funds have a target VaR. First and second round losses have an impact on funds' exposure to risk for two reasons: (1) total exposures are modified, and (2) a loss has already been absorbed. Assuming that market volatility is not influenced by the alignment to a climate policy, we compute the amount of assets that funds have to liquidate in order to go back to their initial VaR level.

Using time series of funds' prices, we estimate the original VaR of fund  $i$   $\text{VaR}(0)_i$ .

Let us define the relative  $\overline{\text{VaR}}$  of fund  $i$  with respect to fund's  $i$  initial total assets

$$\overline{\text{VaR}}_i = \frac{\text{VaR}(0)_i}{A(0)_i}. \quad (16)$$

The new value of assets after first and second rounds is

$$A(2)_i = A(0)_i + \Xi^{1st} + \Xi^{2nd}. \quad (17)$$

While the balance sheet of funds is shrank by the effect of first and second rounds shocks, total losses

induced by market volatility also shift the VaR level towards the left. The new level of VaR thus is

$$\text{VaR}(2)_i = A(2)_i \cdot \overline{\text{VaR}}_i - \Xi_i^{1st} - \Xi_i^{2nd}, \quad (18)$$

where we assumed that the distribution of shocks due to market volatility has not been modified by the climate policy but only depends on the demand and supply dynamics. Since, by construction,  $\text{VaR}(2)_i > \text{VaR}(0)_i$ , each fund  $i$  reacts by liquidating a portion  $k_i$  of its assets. The new value of VaR after liquidation thus reads as

$$\text{VaR}(3)_i = (1 - k_i) \cdot A(2)_i \cdot \overline{\text{VaR}}_i - \Xi_i^{1st} - \Xi_i^{2nd}. \quad (19)$$

Imposing  $\text{VaR}(3)_i = \text{VaR}(0)_i$  one solves for  $k_i$ .

### 2.5.3 Price impact of Fire-Sales

The sudden liquidation of portion of asset classes add downward pressure on asset prices. We assume the price impact function to be similar to the one presented in (Cifuentes et al., 2005). More in detail, the price per units of assets after the liquidation  $p_{cs}^{\text{after}}$  is a function of the relative liquidation  $K_{cs}$  and of the price before the liquidation  $p_{cs}^{\text{before}}$

$$p_{cs}^{\text{after}} = p_{cs}^{\text{before}} \cdot e^{-\alpha \frac{\sum_i A(1)_{ics} k_i}{\sum_i A(1)_{ics}}} = p_{cs}^{\text{before}} \cdot e^{-\alpha K_{cs}}. \quad (20)$$

where  $A(1)_{cs}$  is the value of the sector  $s$  in country  $c$  after the introduction of the climate policy, and  $\alpha$  is the market liquidity.

While liquidating at a higher price, what remains in banks' and funds' balance sheets loses value because of an increase in supply. By defining the relative price drop due to liquidation as

$$\bar{p}_{cs} = \frac{p_{cs}^{\text{after}}}{p_{cs}^{\text{before}}} \quad (21)$$

third round shock is thus written as

$$\Xi_i^{3rd} = \sum_c \sum_s (1 - k_i) \cdot A(1)_{ics} \cdot (1 - \bar{p}_{cs}). \quad (22)$$

Notice that, in the spirit of Greenwood et al. (2015), banks and funds do not account for other institutions reaction. An equilibrium would be reached by iterating the dynamics several times. In order to avoid losses due to asset fire-sales to increase uncontrollably we only compute one liquidation iteration. As discussed in Greenwood et al. (2015), under certain assumptions the dynamics would

converge to a non-zero fixed point. However, given that there is a considerable amount of asset overlapping within the Mexican banking system, we calibrated the Asset Fire-Sales dynamics using a parameter which made less severe the price impact function also because most of the overlapping is caused by the holding of government debt, which are the most liquid securities in the market and which have full government support. In the rest of this project we set market liquidity  $\alpha = \ln 4/3$ . This reflects into a very liquid market since the entire liquidation of an asset class would drop its price to 75% of its initial value.

## 2.6 Losses transferred to external creditors

While banks' external creditors are first in seniority of payments, it is possible that losses are too large to be absorbed by their capital and their interbank liabilities. To compute the amount of losses that is transferred to external creditors, which also include depositors, we reconstruct the balance sheet identity

$$\Xi_i^{4th} = \min \left\{ 0, \Xi_i^{1st} + \Xi_i^{2nd} + \Xi_i^{3rd} + E(0)_i + \sum_j L_{ij}^b \right\}. \quad (23)$$

## 3 Data

The data used for this work comes from many different sources and repositories at Banco de Mexico. After the 1994 financial crisis in Mexico, financial authorities reached a wide consensus on the data to be collected from the financial system and on the mechanisms which would allow them to share such data. For this reason in Mexico there is a comprehensive coverage of the banks' exposures, as well as for some other financial intermediaries.

The exposures considered in this work come from the regulatory reports that the banks' supervisor and the central bank collect from financial intermediaries. This data comprises the following information:

- Banks loans
- Interbank loans and deposits
- Securities holdings of banks, funds and brokerage houses
- Derivatives exposures among banks and brokerage houses
- Interbank foreign exchange transactions



In the following subsections we will provide more detail on each type of exposure and how it was aggregated in order to be used along with the macro model to estimate the impact of climate change in the financial system.

### **3.1 Banks' exposures data**

The data used to compute the exposures of banks and brokerage houses to economic sectors which might be directly affected by the climate change comes from two important sources: i) a regulatory report known as the RC04 which collects all the outstanding loans information (at the loan level) from every bank in Mexico, including development banks at the end of the month; and ii) the holdings of securities of banks (including development banks), brokerage houses and investment funds with a daily frequency.

The individual loan data had already included the NAICS sector code, from there a lookup table which relates the NAICS with the CPRS sectors was built<sup>5</sup>. For the information on securities holdings, it was possible to map each security to a specific sector using the NACE code at four-digits level (obtained in Bloomberg using the ISIN identifier of each issuance).

Once the CPRS sector was assigned to each loan granted and each security held by a bank the exposure to each sector has been computed as the sum by bank and CPRS sector.

### **3.2 Funds' exposures data**

In addition to the information on securities holdings by banks and brokerage houses we also obtained the securities positions for investment funds in Mexico. The procedure to obtain the fund's exposures to different economic sectors was very similar to the banks' case. Having the securities identified by the ISIN code, the NACE code was obtained and from there the mapping between NACE and CPRS was used.

The funds' exposures to banks and brokerage houses was obtained from the same data source that is used to perform the contagion studies at the Mexican central bank.

The VaR used in the fire sales dynamics comes from the empirical quarterly return distribution for each fund (the 90%, 95%, 99% and 99.9% VaR were obtained). The history of available prices is different depending on the individual fund and ranges from December 2008 to December 2018. On average 600 data points were used to calculate each VaR; the funds' prices were obtained using Morning Star. The coverage of the prices was not complete, since only for half of the funds present in our data (around 300) price information was found. In order to fill the gaps the corresponding

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<sup>5</sup>Since the shocks to climate-relevant sectors are known for the LIMITS classification, we created a mapping between both groupings.

VaR was calculated for each confidence level, i.e., the 90% VaR of the 90% VaRs was assigned for the missing funds, and so on.

### **3.3 Interbank exposures data**

The interbank exposures are obtained from an old contagion project at Banco de México. This database consists of the outstanding exposures at the pair-level on a daily frequency for a large number of financial intermediaries, including commercial banks, development banks, brokerage houses and investment funds among others. The exposures are computed considering information from unsecured loans, cross holdings of securities, derivatives and foreign exchange related exposures. This data set has been explained and used in many previous works such as Martinez-Jaramillo et al. (2010), Solorzano-Margain et al. (2013), Martinez-Jaramillo et al. (2014), Poledna et al. (2015), Molina-Borboa et al. (2015), Batiz-Zuk et al. (2016) and Anand et al. (2017) among others.

### **3.4 Banks-Funds' exposures data**

This data also comes from the contagion data set resident at Banco de Mexico, in such database exposures are computed among most of the institutions in the Mexican financial system. In particular investment funds hold banks' securities and in this way are exposed to them.

## **4 Results**

### **4.1 Descriptive statistics of climate relevant exposures**

We first carry out a descriptive statistics of the exposures of financial actors towards the climate policy relevant sectors, CPRS, as defined in the Section Methods. Figure 2 shows the aggregated exposures of banks and investment funds to CPRS in billions of Mexican pesos. The subsectors of the financial sector are grouped together and labelled as "Finance" and include exposures of banks on interbank loans. The remaining sectors are grouped and labelled as "Other" and include a large portion of investments in Mexican sovereign bonds. In the following sections, we will examine how shocks on the CPRS impact directly or indirectly on banks and funds. We will see that while exposures to CPRS determine the first round of losses, interbank loans determine the second round of the contagion process and exposures to sovereign bonds play a role in the third round. Figure 3 shows the relative exposures to CPRS of banks and investment funds as percentage of their respective total assets.

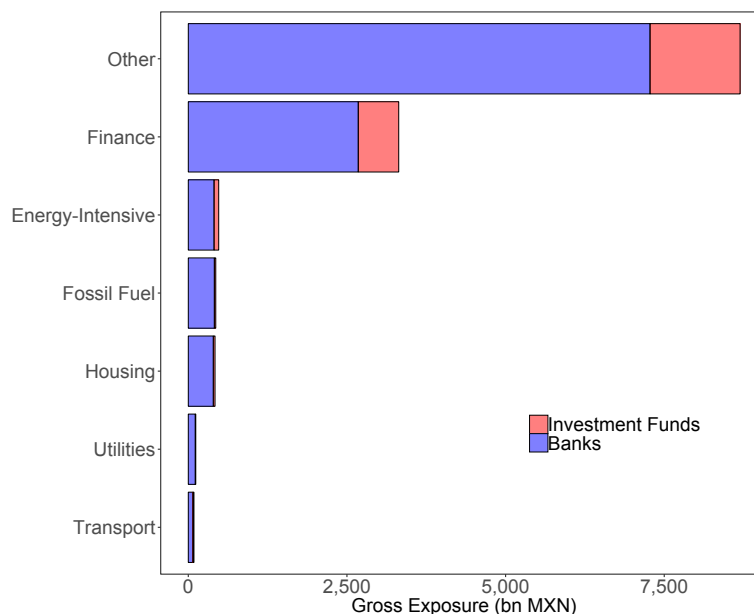


Figure 2: **Exposures to CPRS sectors of banks and investment funds in billions of Mexican pesos.** The x-axis shows banks’ and funds’ gross exposures, in billions of Mexican pesos, towards the Mexican sectors. The y-axis lists the sectors to which banks and funds are exposed, sorted per size. To compare the size of CPRS sectors to the actual size of banks’ and funds’ balance sheets, we included also the sector “Finance” and the sector “Other”, where we put everything which is not included in the CPRS taxonomy. The overlap on those sectors will play a major role on the fire-sales dynamics. Blue bars show the banks’ exposures, red bars show funds’ exposures.

The above figures show that banks’ and funds’ exposures to CPRS are very small in comparison to the Other and Finance sectors. They are also smaller in comparison to similar analysis carried out for EU banks (Battiston et al., 2017). This finding may be surprising considering the fact that the contribution to GVA of the sectors included in the CPRS sectors fossil and utility is at least as large as in the EU. Some explanations comes from specific features of the Mexican economy. The largest oil and the electricity generation companies in Mexico (i.e. PEMEX<sup>6</sup> and CFE<sup>7</sup>) are state-owned. We do observe some loans of banks in these companies as well as investments in corporate bonds. However, these companies receive most funding from the state and thus these exposures do not appear in the dataset. In turn, banks are heavily exposed to sovereign bonds. A possible way to estimate the indirect exposures of banks to PEMEX and CFE would be to compute how much of the funds from the issuance of Mexican sovereign bonds was deployed to fund such companies. Unfortunately, this estimation is not possible at this stage. Moreover, loans that could be related to the transport sector (e.g. to carry out private transportation business) might be classified as loans to households due to

<sup>6</sup>Petróleos Mexicano

<sup>7</sup>Federal Electricity Commission

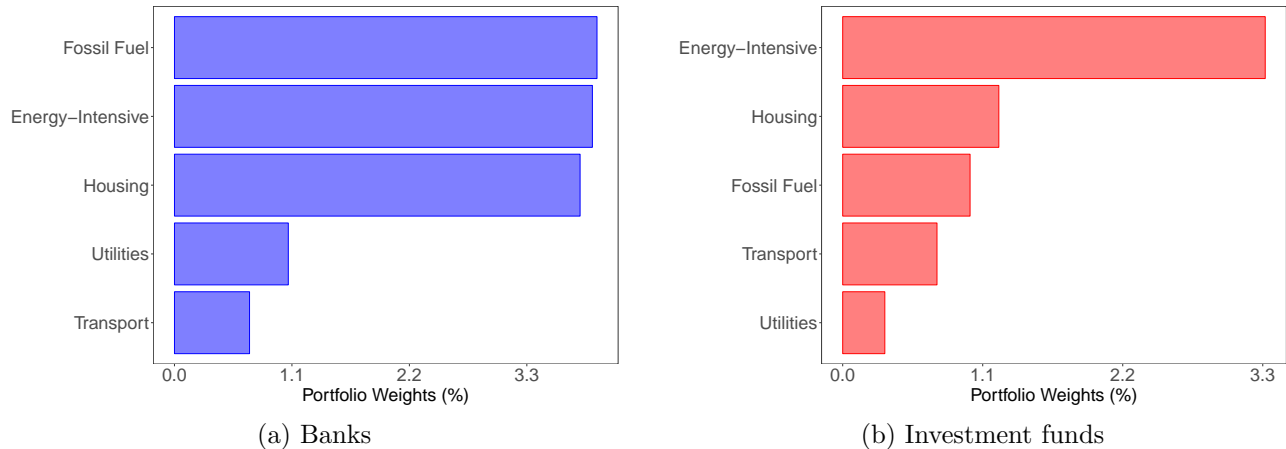


Figure 3: **Break-down of the exposures to CPRS sectors for banks and investment funds relative to total assets.** The x-axis shows the exposure, relative to total assets, towards firms resident in Mexico and operating in the CPRS sectors. The y-axis lists the CPRS sectors to which banks and funds are exposed, sorted by relative exposure. **Left:** banks’ portfolio composition. **Right:** investment funds’ portfolio composition.

the large role of the informal economy in the overall Mexican economy.

## 4.2 Mild Scenario

We recall from the Section 2, that in this paper we refer to a shock scenario the combination of: i) a *market conditions scenario* i.e., a range of values for the parameters recovery rate  $R$ , market volatility  $\sigma$ , market elasticity  $\alpha$ , and the funds’ VaR; and ii) a *climate policy shock scenario*, i.e., a set of shock arising from the late and disorderly alignment from BAU trajectory to a set of climate target trajectories.

We first focus on a mild shock scenario determined by the switch, estimated under the GCAM model, between two policy scenarios, namely from the business-as-usual climate policy (no policy) to the LIMITS-Ref-Pol-500 scenario (see Appendix for a description of the climate policies scenarios). The parameters are set as follows: interbank recovery rate coefficient  $R = 0.5$ , market volatility  $\sigma = 1.0$ , market liquidity  $\alpha = \ln 4/3$ , and funds’  $VaR = 1\%$ . Figure 4 shows the total losses in the financial system (banking sector and investment funds altogether) in Mexican pesos triggered by a disorderly realignment from the policy scenario BAU to LIMITS-RefPol-500, estimated with the model GCAM. The x axis represents time in period of 5 years, along the climate policy scenarios. The y axis represent the magnitude of the losses in billion of Mexican pesos that would occur in all the stages of the financial contagion modelled, as described in the Section Methods.

It is important to understand the correct meaning of the time dimension in this figure. The time

scale of the climate stress-test is meant here to be in relatively short term, about 6 months. The time evolution displayed here, refers to the evolution of the magnitude of the expected losses, conditional to the shock at the same given period. The magnitude of the shock evolve in time because the climate policy trajectories evolve over the years and some tend to diverge. For instance, switching disorderly from BAU to LIMITS-Ref-Pol-500 implies a bigger shock if this happens in 2050 than if this happens in 2025. Figure 5 shows the losses for banks in percentage of regulatory capital (left), and for funds in percentage of total assets (right) under the same scenario and parameters. The first round losses are relatively small. For instance in 2030 they represent about 2% of capital for banks and about 0.2% of total assets for funds.

However, direct financial contagion due to bilateral contracts among banks amplifies the losses suffered by banks and funds by a factor that is approximately 2. This result can be observed comparing the red and orange surfaces in Figures 5. Notice that the second-round stage, i.e. the interbank credit contagion, is modelled using the NEVA framework. As described in the Section 2, this means that, by varying the parameters of recovery rate coefficient  $R$  and the asset price volatility  $\sigma$ , we move smoothly between the two paradigmatic models of financial contagion, from EN to DR. In particular, for intermediate values of these parameters, i.e.  $R > 0$  and  $\sigma > 0$ , the recovery rate is endogenous as in EN, i.e. the fix point of the clearing payment process, but it is combined with bankruptcy costs (the lower  $R$ , the larger the costs) and with risk on the external assets of banks.<sup>8</sup> The final value of interbank assets with face value  $A_{ij}^b$ , is then equal to  $A_{ij}^b \mathbb{V}_{ij}(T)$ , where  $\mathbb{V}_{ij}(T)$  is the network coherent valuation function at the equilibrium of the process that considers future shocks arising from market volatility. Although we consider a very liquid market (i.e.  $\alpha = \ln 4/3$ ), for banks the third round, due to contagion via common exposures, amplifies approximately by a further factor 2 the compound losses of first and second rounds. For funds, the amplification factor effect is larger and approximately 7.

### 4.3 Adverse Scenarios

We then consider some more adverse but still plausible shock scenario. We now use the WITCH model, to estimate the impact of switching from the business-as-usual climate policy (no policy) to four different possible climate policy scenarios (LIMITS-RefPol-500, LIMITS-StrPol-500, LIMITS-RefPol-450, LIMITS-RefPol-500, see Appendix). The labels RefPol versus StrPol refer instead to the timing of the CO2 emission reduction trajectory under the corresponding climate policy scenario. The smaller is the target level of the CO2 concentration in the atmosphere (450 or 500 parts per million),

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<sup>8</sup>Note the distinction between recovery rate, i.e. the fraction of the face value of interbank claims recovered after interbank assets clearing, and the recovery rate coefficient  $R$ , i.e. the fraction that can be recovered net of bankruptcy cost.

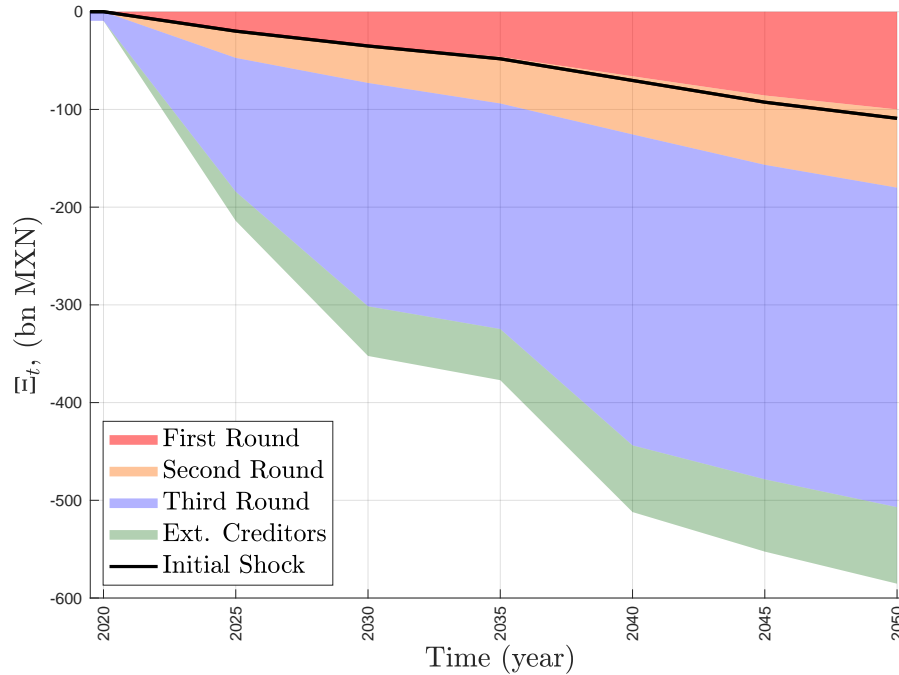


Figure 4: **Profile of losses suffered by the Mexican financial system conditional upon the policy scenario LIMITS-RefPol-500(GCAM).** The x axis represents time in years, along climate policy scenarios. The y axis represent the magnitude of the losses in billions of Mexican pesos. Effect of a shock on the Mexican financial system triggered by a disorderly realignment from the policy scenario BAU to LIMITS-RefPol-500, estimated with the model GCAM. We set interbank recovery rate coefficient  $R = 0.5$ , and market volatility  $\sigma = 1.0$ , market liquidity  $\alpha = \ln 4/3$ , and funds  $VaR = 1\%$ . The solid black lines shows the loss on the asset classes. The red surface shows losses suffered by the Mexican financial system due to direct exposure, the orange surface shows the losses suffered by the Mexican financial system due to direct contagion, the blue surface shows the losses suffered by the Mexican financial system due to indirect contagion, and the green surface shows the losses suffered by creditors of banks which are external to the Mexican financial system.

the more stringent is the climate policy and therefore the larger is the shock in market share affecting the economic sectors. The four climate policy shocks refer here to the switch, estimated under the WITCH model, from the business-as-usual climate policy (no policy) to one of the four climate policy scenario, respectively.

As one may expect, if the parameters of the financial contagion process are the same, the larger the climate policy shock the larger the losses incurred by banks and funds at each stage of contagion. Indeed, the losses computed by the contagion model in each stage are a non decreasing function of the magnitude of the initial shock. Figure 6 illustrates this fact by comparing the total losses in the financial system in millions of Mexican pesos. On the left, we consider the shock of switching

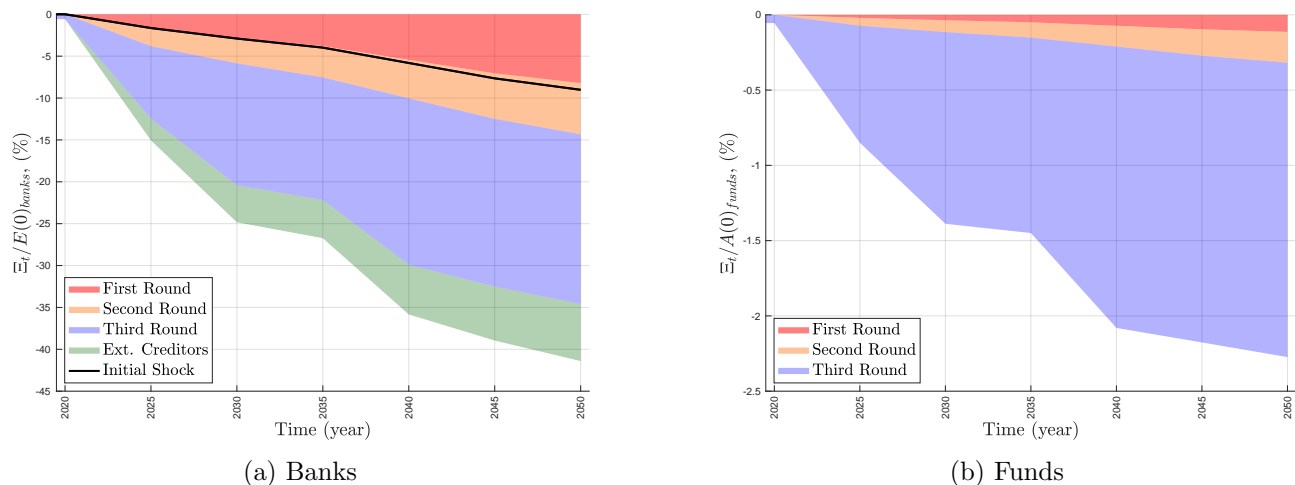


Figure 5: **Break down of shock on banks and funds triggered by the policy scenario LIMITS-RefPol-500(GCAM)**. The red surface shows the shock due to direct exposure, the orange surface shows the shock due to direct contagion, the blue surface shows the shock due to indirect contagion, and the green surface shows the losses suffered by creditors of banks which are external to the Mexican financial system. The solid black lines shows the loss on the asset classes. **Left:** the shock suffered by Mexican banks. **Right:** the shock suffered by Mexican funds. We have set interbank recovery rate  $R = 0.5$ , market volatility  $\sigma = 1.0$ , market liquidity  $\alpha = \ln 4/3$ , and funds  $VaR = 1\%$ .

disorderly from BAU to StrPol500. On the right, we consider the shock of switching disorderly from BAU to StrPol450, which is stricter than StrPol500. The meaning of the time periods is the same as in the previous figures. The parameters are set as follows: interbank recovery rate coefficient close to  $R = 0.5$ , market volatility close  $\sigma = 0.8$ , market liquidity  $\alpha = \ln 4/3$ , and funds'  $VaR = 1\%$ .<sup>9</sup>

As we can see, in each time period, the losses in the second scenario are larger or equal than in the first. This is due to the fact that losses due to direct exposure, shown by the red surface, are larger in the stricter policy scenario than in the more conservative one. While initial losses are then amplified by the same market conditions, total losses in the policy scenario StrPol-450 are always larger than total losses in the policy scenario StrPol-500.

Milder or more adverse climate policy scenarios are not the only determinant of the systemic losses in our model. The interplay between climate policy shock scenarios and financial market conditions is crucial. A milder climate policy shock could lead to larger losses if the market conditions are worse enough. This is illustrated in Figure 7. We consider two cases. On the left, the climate policy shock scenario StrPol500 is milder but the market conditions are harsher. Indeed, a lower recovery rate coefficient implies larger losses in the interbank network, conditional upon default of

<sup>9</sup>Notice that strictly speaking, because the parameters  $R$  and  $\sigma$  are drawn from a Beta distribution, we could select two scenarios with values of  $R$  and  $\sigma$  that are very close but not identical. In detail,  $R$  is drawn from a beta distribution with parameters  $\beta(4, 2)$ , and  $\sigma$  is drawn from a beta distribution with parameters  $\beta(5, 2)$

counterparties. Larger asset price volatility implies lower expected value of bonds. We observe, that losses are systematically larger in the first case than in the second. Additionally, notice that losses triggered by the climate policy StrPol500 in the year 2030 are about the same as losses triggered by the climate policy StrPol450 around year 2023. This implies that, under the same market conditions, an *early*, but still disorderly, alignment to *more demanding* climate targets could have the same impact on the financial system as a *late* and disorderly alignment to *less demanding* climate targets.

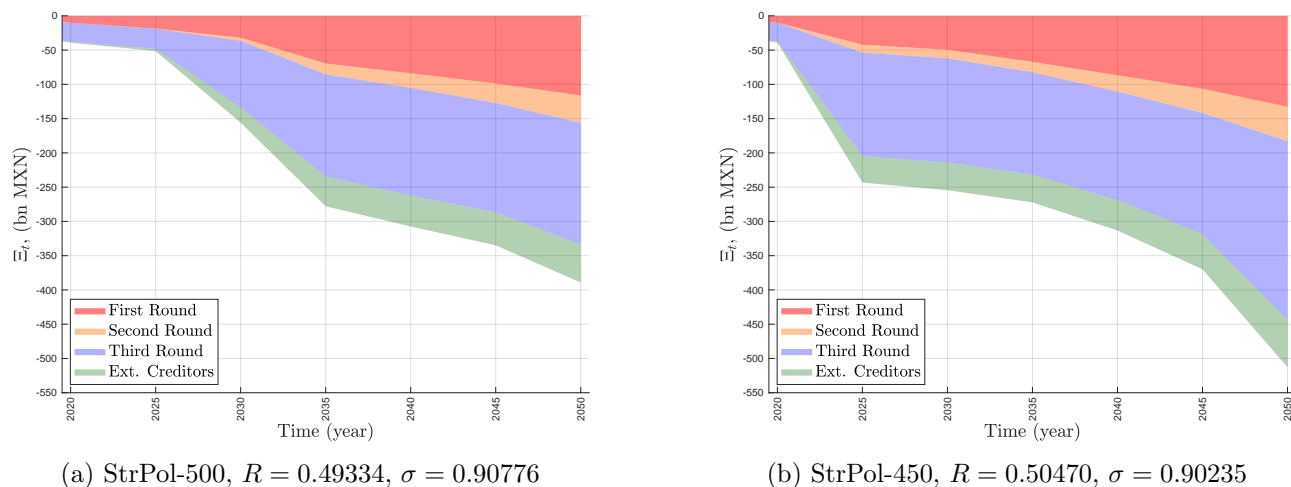


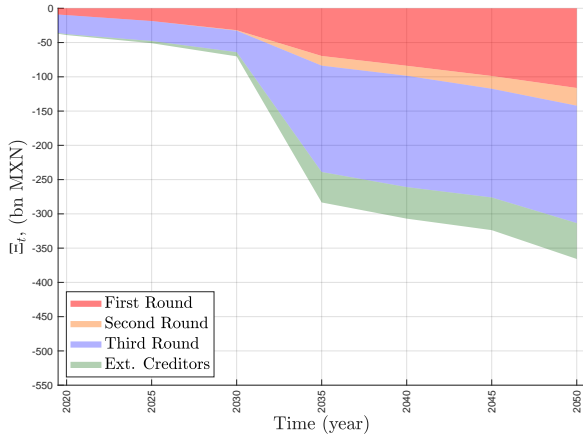
Figure 6: **Comparison of shock suffered by the Mexican financial system in the two different policy scenarios estimated using the WITCH model.** Among all trajectories, we have selected two that have interbank recovery rate  $R$  close to  $R = 0.5$  and market volatility  $\sigma$  close to 0.9. Further, we have set market liquidity  $\alpha = \ln 4/3$ , and funds'  $VaR = 1\%$ . The red surface shows losses suffered by the Mexican financial system due to direct exposure, the orange surface shows the losses suffered by the Mexican financial system due to direct contagion, the blue surface shows the losses suffered by the Mexican financial system due to indirect contagion, and the green surface shows the losses suffered by creditors of banks which are external to the Mexican financial system.

#### 4.4 Sensitivity analysis

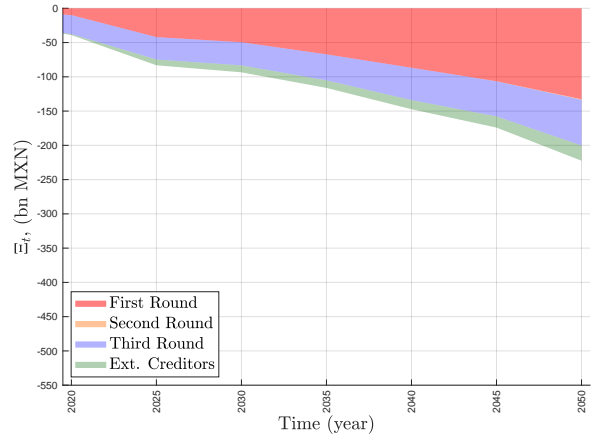
The interplay between climate policy shock scenarios and market conditions leads to the fact that the magnitude of systemic losses in the financial system is a multi-dimensional surface that depends in a non monotonic way on the parameters.

In each climate policy shock scenario, the losses can vary substantially across the market conditions (i.e. for varying levels of recovery rate  $R$  and asset price volatility  $\sigma$ ). A first method to provide actionable insights for financial stability, is to characterize the interplay by means of a sensitivity analysis. We focus on the WITCH model and we compare losses at each stage of the contagion process across the parameter space, by varying the recovery rate, the market volatility and the climate policy shock scenarios. The results are reported in Table 2, which can be read as follows. For each year





(a) StrPol-500,  $R = 0.39607$ ,  $\sigma = 0.80354$



(b) StrPol-450,  $R = 0.78736$ ,  $\sigma = 0.38525$

**Figure 7: Comparison of shocks suffered by the Mexican financial system in two different amplification scenarios.** Among all trajectories, we have selected two. **Left:** a mild policy scenario with strict recovery rate  $R$  close to 0.4 and market volatility  $\sigma$  close to 0.8. **Right:** a strict policy scenario with conservative recovery rate  $R$  close to 0.8 and market volatility  $\sigma$  close to 0.4. In both scenarios, we have set market liquidity  $\alpha = \ln 4/3$ , and funds'  $VaR = 1\%$ . The red surface shows losses suffered by the Mexican financial system due to direct exposure, the orange surface shows the losses suffered by the Mexican financial system due to direct contagion, the blue surface shows the losses suffered by the Mexican financial system due to indirect contagion, and the green surface shows the losses suffered by creditors of banks which are external to the Mexican financial system.

and scenario, we report the values of the shocks on the fossil fuel and utility sectors (corresponding as before to a disorderly switch from a BAU scenario to the chosen climate policy scenario). For instance, in line 15 of Table 2, the shock on the fossil fuel sector and utility sector corresponding to a disorderly switch from BAU to the climate policy scenario StrPol450 are about  $-15\%$  and  $-59\%$ , respectively. The first round loss is  $0.31\%$  of total asset. Along the columns, from the second round on, we report the Climate Value at Risk for each round of the climate stress test, computed across the realisation of the parameters. Indeed, to analyse the impact of uncertainty on recovery rate and market volatility on the profile of losses suffered by the Mexican financial system relative to initial total assets, for each of the four policy scenarios, we have generate a set of 1000 trajectories. Each trajectory is characterized by a value of the recovery rate  $R$  drawn from a Beta distribution with parameters  $\beta(4, 2)$  and a market volatility  $\sigma$  also drawn from a beta distribution with parameters  $\beta(5, 2)$ . For each time period, we then compute the value at risk, in the following referred to as VaR, with a given confidence level  $p$  across the set market conditions. The VaR is defined as the value of the loss such that losses larger than VaR occur with probability smaller than  $p$ . For instance, again on line 15 of the Table 2, the figures imply that, given the policy scenario StrPol-450 estimated with the model WITCH, the Mexican financial system has  $1\%$  probability to lose at least  $1.34\%$  of its total

assets after third round, under the assumptions that interbank recovery rate and market volatility are drawn from Beta distributions with the parameters discussed above.

#### 4.4.1 Climate Scenario Envelope Analysis

A second, more intuitive, method to provide actionable insights for financial stability from the multi-dimensional surface of systemic losses is what we call here a *climate scenario envelope analysis*.

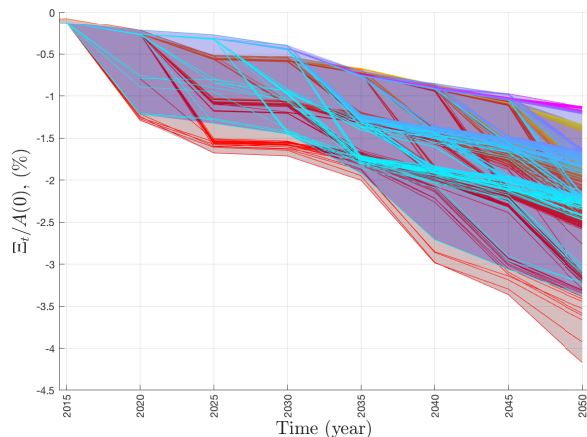
We then define an *envelope of trajectories* as follows. First we consider the subset of trajectories obtained when the parameters related to both climate policy shocks and market conditions (recovery rates, market volatility, market elasticity) are confined with some specified ranges. Second, the envelope of trajectories is the surface bounded by the minimum and maximum shocks at each time period.

In Figure 8a we show two climate envelopes one above the other. The upper climate envelope, highlighted in blue color code, illustrates the profile of losses in a mild scenario where the climate policy scenario is less demanding (RefPol-500). The second climate envelope, highlighted in red color code, illustrates the profile of losses in a scenario where the climate policy scenario is more demanding (RefPol-450). Additionally, inside each envelope, we show each individual trajectory of losses. The figure shows that, while one policy scenario is more stringent than the other, the interplay with market conditions creates a large surface where the two envelopes overlap. All climate policy shocks have been estimated using the WITCH model and we set market liquidity  $\alpha = \ln 4/3$  and funds  $VarR = 1\%$ . Since recovery rate  $R$  and market volatility  $\sigma$  are drawn from Beta distributions the upper and lower bound coincide to the losses estimated with well established models of financial contagion. The upper bound corresponds to the (Eisenberg and Noe, 2001) estimation (i.e., when  $R = 1$  and  $\sigma = 0$ ). The lower bound corresponds to the (Battiston et al., 2012b) estimation (i.e., when  $\sigma = 1$ ) with recovery rate  $R = 0$ .

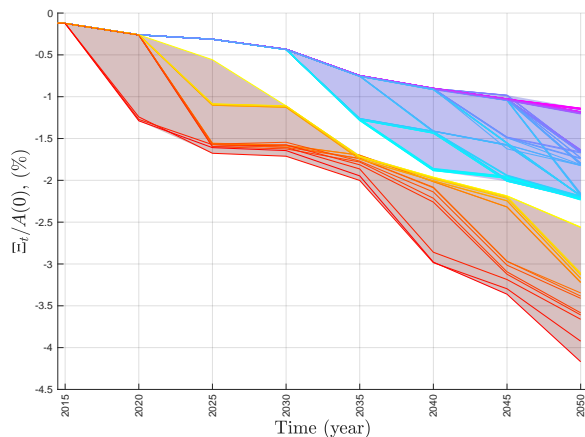
On Figure 8b we only show the subset of trajectories that are within specific ranges of market conditions. Trajectories in the blue envelope are such that recovery rate  $R$  is between 0.4 and 0.8, and market volatility  $\sigma$  is between 0.6 and 0.8. Indeed, a high recovery rate and a low market volatility lead to lower level of amplification losses in the contagion process Roncoroni et al. (2018). Trajectories in the red envelope are such that recovery rate  $R$  is between 0.8 and 1.0, and market volatility  $\sigma$  is between 0.0 and 0.4. More adverse market conditions are such that amplification of losses is larger. Because total losses are non decreasing when recovery rate  $R$  decreases, market volatility  $\sigma$  increases, or the climate policy shock becomes more negative we managed define two envelopes that are disjoint. This can always be reached by selecting ranges for market conditions that are non overlapping. Because in the blue envelope market volatility is low, loss amplification starts late in time and has a small effect due to large recovery rate. In fact, the shock only reach 2% of total assets. Because in the red

envelope market volatility is large, loss amplification starts early in time and has a large effect due to low recovery rate. The initial shock is amplified up to more than 4% of total assets.

The climate envelope scenario analysis is thus a simple graphic method that can be used to compare bundles of trajectories across a wide range of climate policy scenarios and market conditions scenarios.



(a) RefPol-500 and RefPol-450 envelopes.



(b) RefPol-500 and RefPol-450 envelopes, comparison of market conditions.

Figure 8: **Climate Scenario Envelope Analysis of two climate policy scenarios.** The first envelope is highlighted in color code **blue** and is characterized by the LIMITS trajectory of the policy scenario LIMITS-RefPol-500. The second envelope is highlighted in color code **red** and is characterized by the LIMITS trajectory of the policy scenario LIMITS-RefPol-450. The figure on the **left** shows the entire set of trajectories while the figure on the **right** focuses on two specific market condition scenarios. In particular, each trajectory in the blue envelope corresponds to a market volatility  $\sigma$  between 0.6 and 0.8, and an interbank recovery rate  $R$  between 0.4 and 0.8. Each trajectory in the red envelope corresponds to a market volatility  $\sigma$  between 0.8 and 1.0, and an interbank recovery rate  $R$  between 0.0 and 0.4. The color of each trajectory has been chosen to highlight the ranking of losses at year 2050. All climate policy shocks have been estimated using the WITCH model and we set market liquidity  $\alpha = \ln 4/3$  and funds  $VaR = 1\%$ .

## 5 Conclusion and Policy Implications

In this paper we extend the framework of the climate stress test of the financial system to analyze the effects on financial stability of the interplay of climate policy shocks and market conditions.

We develop a climate stress test framework to estimate the direct and indirect impact of a late and disorderly alignment to climate targets. We consider a financial system composed of banks and investment funds. The methodology combines the estimation of losses arising both from interbank distress contagion as well as from common asset exposures. The valuation of interbank claims is

carried out before maturity and accounts for the endogenous (i.e., network coherent) recovery rate of banks Eisenberg and Noe (2001); Battiston et al. (2012b); Barucca et al. (2016). Contagion via common exposures assumes a reaction of financial institutions in order to get to the initial balance sheet constraints Kiyotaki and Moore (2002); Caballero and Simsek (2013); Greenwood et al. (2015).

We then apply our methodology to a supervisory dataset including the exposures of the Mexican banks and investment funds to climate policy relevant sectors. We observe small direct exposure to climate policy relevant sectors (in particular to fossil utility and transportation), however this may be due in part to the specific characteristics of the Mexican economy (e.g., the level of informality of the economy, see Section 4.1).

For our climate stress-test we consider climate scenarios that are a combination of climate policy shocks scenarios and market conditions scenarios. Despite the small direct exposure, we identify climate policy scenarios and market conditions where losses due to financial contagion are large.

In a mild scenario (i.e., transition towards a less demanding climate targets, and market conditions characterized by a lower levels of risk), we find losses ranging between 1% and 2% of total assets of the Mexican financial system. In a more adverse scenario (i.e. where the climate policy scenario is more stringent and triggers a negative shock of larger magnitude, and market conditions are such that amplification is larger) we find that systemic losses range between 2.5% and 4% of initial total assets. Our findings show that the total losses for the financial system result from the interplay between climate policy shocks and market conditions. Finally, we develop a graphic method to compare the levels of financial stability under different climate policy scenarios in a range of market conditions.

Our results have three main policy implications. As we have seen, in the mild shock scenario the systemic losses are relatively contained but losses increase when the disordered alignment to climate targets occurs later in time. Thus the first policy implication is that, if the alignment of the real economy to climate targets cannot be avoided to be disorderly, then financial institutions have an incentive for such an alignment to occur as early as possible because financial losses would be smaller.

Further, a late and disorderly transition to a mild climate policy shock scenario implies relatively large losses for the financial system. However, under the same market conditions, the disorderly transition to a stricter scenario may lead to the same level of losses if the alignment occurs earlier. The second policy implication is that a country could reach a more stringent climate target, if the alignment occurs earlier, at the same cost (in terms of financial losses) of reaching a less stringent target with a later alignment.

Finally, we show that aligning to a milder climate policy scenario might lead to larger losses than aligning to a more stringent climate policy scenario if market conditions are riskier. Thus, the third policy implication is that in the face of a tighter climate policy shock, it is possible to contain the adverse effect of financial contagion if the market conditions are strengthened enough.

Several limitations apply to our data and to our model, which should be taken into account when considering the results and their policy implications.

A first limitation of our model, is that it assumes a mechanic transmission of the shock along chains of financial contracts which are taken as exogenous and constant in time. For instance, conditional to the shock, the banks suffer a loss on their balance sheet without being able to anticipate the loss and reallocate their portfolio. Further, its loss translates in a decrease in value of the obligation it has issued on the interbank credit market, thus propagating the loss to its counterparties. Again, the counterparties are not able to anticipate and avoid this loss. Nonetheless, this approach is common to most models of financial contagion in the interbank market and similar approaches have been long used for policy purposes Henry and Kok (2013). As demonstrated by the financial events of 2008, as well as by the policy events of the recent years (e.g. Brexit, Paris Agreement achievement, US withdrawal from Paris Agreement), market players are not always able to anticipate shocks nor to rebalance in time their portfolios of interbank contracts. In particular, they do not have full information on the network of contracts among counterparties. The value of this approach is to estimate the losses for the financial system in severe yet plausible scenarios that while stylized may provide insights on the upper bounds of the losses in paradigmatic situations.

A second limitation regard the third stage of the contagion process, i.e. the fire sales. While agents do react to the shock by trying to maintain their risk management targets (leverage for banks and Value at Risk for funds), they do not internalize the impact of their own reaction and other agents' reaction. However, if they did, this would lead to an overall larger drop in asset price values. Therefore, this assumption implies a conservative estimate of the losses to sudden liquidation of common assets. Notice that this feature applies also to established models of common asset contagion Caccioli et al. (2014); Greenwood et al. (2015).

A third limitation concerns the probability distribution of idiosyncratic shocks on banks' external assets occurring between the time of valuation and the time of the maturity. While a uniform distribution of shocks is unrealistic, it represents an upper bound on the tails of the loss distribution of a defaultable bond (see discussion in Section 2.4). Future work should addressing this limitation empirically calibrating the distribution of stochastic shocks induced by market volatility.

A fourth limitation regards the fact that a large portion of the holdings of banks and funds consists of sovereign bonds. Their value is indirectly affected by climate policy shocks because they may decrease their fiscal revenues and thus decrease the sovereign's ability to pay the coupons and the face value (Battiston and Monasterolo, 2019).

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## A Summary of losses due to direct and indirect contagion

In this section we summarize losses due to contagion in different policy scenario and under different market conditions. The two tables show, for each scenario and model the relative shock to the climate relevant sectors, losses suffered by banks in the three stages of contagion expressed as percentage of total initial investment and gross losses suffered by external creditors expressed in thousands of Mexican pesos. For all results, we set market liquidity  $\alpha = \ln 4/3$  and funds  $VaR = 1\%$ . Each statistics refers to 500 realizations where market volatility  $\sigma$  has been randomly generated following a beta distribution with parameters  $\beta(5, 2)$  and recovery rate has been generated following a beta distribution with parameters  $\beta(4, 2)$ . For instance, line 31 shows that the WITCH model estimates that the introduction of the StrPol-450 policy scenario would decrease by 51.68% the value to loans to the sector Fossil-Fuel. Similarly, the loans granted to the the Utilities sector would lose 79.05% of their value. Those two shocks would trigger a devaluation of assets of the Mexican financial system due to direct exposure equal to 0.82%. 1% of the realizations, financial contagion due to direct exposure would further decrease the value of total assets of the financial system of 1.24%. Further, financial contagion due to liquidation of common assets would decrease the value of total assets of the Mexican financial system of 2.87%. Finally, the losses that are too large to be absorbed by banks' capital and is transmitted to external creditors is 3.30% of banks' initial capital.

Index	Year	Model	Scenario	Fossil Fuel shock	Utilities shock	1 <sup>st</sup> Round	2 <sup>nd</sup> Round VaR1%	3 <sup>rd</sup> Round VaR1%	Ext. VaR1%
1.	2015	WITCH	RefPol-450	0.17	-0.71	-0.01	-0.01	-0.12	-0.12
2.	2015	WITCH	RefPol-500	0.17	-0.71	-0.01	-0.01	-0.12	-0.12
3.	2015	WITCH	StrPol-450	0.18	-0.78	-0.01	-0.01	-0.13	-0.13
4.	2015	WITCH	StrPol-500	0.18	-0.78	-0.01	-0.01	-0.13	-0.13
5.	2020	WITCH	RefPol-450	-0.37	-5.69	-0.08	-0.09	-0.26	-0.27
6.	2020	WITCH	RefPol-500	-0.37	-5.69	-0.08	-0.08	-0.25	-0.27
7.	2020	WITCH	StrPol-450	-0.80	-10.73	-0.06	-0.06	-0.23	-0.24
8.	2020	WITCH	StrPol-500	-0.80	-10.73	-0.06	-0.06	-0.23	-0.24
9.	2025	WITCH	RefPol-450	-6.37	-49.01	-0.28	-0.39	-1.32	-1.57
10.	2025	WITCH	RefPol-500	-2.33	-32.53	-0.11	-0.18	-0.78	-0.90
11.	2025	WITCH	StrPol-450	-5.67	-45.90	-0.26	-0.35	-1.28	-1.52
12.	2025	WITCH	StrPol-500	-2.33	-31.40	-0.11	-0.14	-0.73	-0.84
13.	2030	WITCH	RefPol-450	-15.30	-59.27	-0.30	-0.42	-1.34	-1.59
14.	2030	WITCH	RefPol-500	-7.57	-35.45	-0.20	-0.29	-1.22	-1.44
15.	2030	WITCH	StrPol-450	-14.73	-58.31	-0.31	-0.41	-1.34	-1.59
16.	2030	WITCH	StrPol-500	-7.50	-35.55	-0.20	-0.27	-1.19	-1.42
17.	2035	WITCH	RefPol-450	-23.44	-64.54	-0.42	-0.59	-1.52	-1.77
18.	2035	WITCH	RefPol-500	-14.60	-35.75	-0.43	-0.59	-1.51	-1.78
19.	2035	WITCH	StrPol-450	-22.84	-63.23	-0.41	-0.55	-1.49	-1.75
20.	2035	WITCH	StrPol-500	-14.32	-35.36	-0.43	-0.55	-1.50	-1.78
21.	2040	WITCH	RefPol-450	-32.22	-69.44	-0.54	-0.80	-1.85	-2.13
22.	2040	WITCH	RefPol-500	-20.33	-38.02	-0.52	-0.74	-1.72	-2.00
23.	2040	WITCH	StrPol-450	-31.60	-68.19	-0.53	-0.74	-1.78	-2.06
24.	2040	WITCH	StrPol-500	-20.00	-37.58	-0.52	-0.69	-1.66	-1.93
25.	2045	WITCH	RefPol-450	-41.20	-74.53	-0.66	-1.01	-2.60	-2.99
26.	2045	WITCH	RefPol-500	-26.65	-41.97	-0.61	-0.92	-2.01	-2.33
27.	2045	WITCH	StrPol-450	-40.35	-73.32	-0.66	-0.96	-2.55	-2.93
28.	2045	WITCH	StrPol-500	-26.26	-41.42	-0.61	-0.84	-1.84	-2.14
29.	2050	WITCH	RefPol-450	-52.54	-80.06	-0.82	-1.28	-2.91	-3.35
30.	2050	WITCH	RefPol-500	-34.87	-48.66	-0.72	-1.11	-2.73	-3.15
31.	2050	WITCH	StrPol-450	-51.68	-79.05	-0.82	-1.24	-2.87	-3.30
32.	2050	WITCH	StrPol-500	-34.22	-47.85	-0.72	-1.02	-2.60	-3.00

Table 2: Summary of evolution in time contagion for a given model and scenario